

Scalable Optimization of Multivariate Performance Measures in Multi-instance Multi-label Learning

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Abstract

The problem of multi-instance multi-label learning (MIML) requires a bag of instances to be assigned a set of labels most relevant to the bag as a whole. The problem finds numerous applications in machine learning, computer vision, and natural language processing settings where only partial or distant supervision is available. We present a novel method for optimizing multivariate performance measures in the MIML setting. Our approach $MIML^{perf}$ uses a novel plug-in technique and offers a seamless way to optimize a vast variety of performance measures such as macro and micro-F measure, average precision, which are performance measures of choice in multi-label learning domains. $MIML^{perf}$ offers two key benefits over the state of the art. Firstly, across a diverse range of benchmark tasks, ranging from relation extraction to text categorization and scene classification, $MIML^{perf}$ offers superior performance as compared to state of the art methods designed specifically for these tasks. Secondly, $MIML^{perf}$ operates with significantly reduced running times as compared to other methods, often by an order of magnitude or more.

1 Introduction

The paucity of labeled data has fueled much interest in learning paradigms with partial or *distant* supervision. The task of Multi-instance Multi-label (MIML) learning is one such paradigm that has received much attention in areas such as relation extraction (RE), image classification etc. The problem requires a bag of data points to be assigned a set of labels most relevant to the bag as a whole. To take an example, in the RE setting, we are interested in identifying relations held by entities being discussed in a body of text. The problem is pretty straightforward in the presence of sentence level annotations *i.e.*, indications of which sentences discuss specific relations. However, this requirement is a prohibitive one, especially when the number of relations runs into the hundreds or thousands. Consequently, the problem is often posed as that of learning under distant supervision (Haffari, Nagesh, and Ramakrishnan 2015; Hoffmann et al. 2011; Surdeanu et al. 2012; Zeng et al. 2015) wherein one is pro-

vided only with relational facts in a database along with a non-annotated corpus that overall, supports most of the facts.

The general MIML problem has been explored through reductions to single instance or single label learning in the past (Zhou and Zhan 2006; Zhan and Zhou 2008). The RE problem has enjoyed more focused attention and several diverse approaches have been proposed for this problem such as structural risk minimization Hoffmann et. al. (2011), neural networks (Zeng et al. 2015) and graphical models (Surdeanu et al. 2012).

Existing approaches for the MIML problem suffer from two main drawbacks 1) Although performance measures such as F-measure and average precision are standard for evaluation, the algorithms do not seek to optimize them directly, instead choosing to adopt heuristics that encourage good performance. An exception is the work of Haffari et al. (2015) who attempt to directly optimize the F-micro measure. 2) The algorithms are often expensive in terms of training time and cannot scale to large, web-scale datasets.

We address both these issues by developing $MIML^{perf}$, a *plug-in* classifier for the MIML problem. $MIML^{perf}$ directly tries to optimize complex performance measures such as macro and micro-F measure in a scalable manner. $MIML^{perf}$ excels over its competitors in its ability to predict rare labels correctly. A notable feature of $MIML^{perf}$ is its streaming nature, that allows it to be executed by making several passes over the data without the need for storing the entire dataset in memory. We rigorously benchmark $MIML^{perf}$ to establish that 1) it offers far greater label extraction accuracies on RE than specialized methods for the problem, 2) it also outperforms state-of-the-art MIML approaches on text categorization and scene classification problems, and 3) it can offer orders of magnitude faster running times.

2 Related Work

Completely supervised approaches, such as those for RE (Zhou et al. 2005; Surdeanu and Ciaramita 2007) have limited application owing to their requirement of fully annotated data which is expensive. Of the alternate paradigms, that of *distant supervision* has found much appeal in both RE and MIML literature. For the RE problem, this paradigm shift due to (Mintz et al. 2009) fueled much interest with

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(Riedel, Yao, and McCallum 2010; Yao, Riedel, and McCallum 2010) modeling the problem as that of mapping entity pairs in the database to their mentions in the corpus, in other words, a multi-instance single-label learning problem. Soon, (Hoffmann et al. 2011; Surdeanu et al. 2012) generalized this to allow entity pairs to participate in multiple relations, thus completing the MIML abstraction. A variety of techniques have been applied to this problem over the years. Recently (Zeng et al. 2015) applied Piecewise Convolutional Neural Networks (PCNNs) to the RE problem. However, these models were often trained by optimizing performance measures such as conditional log-likelihood (Surdeanu et al. 2012), error rate, or bag level entropy (Zeng et al. 2015) that are not directly related to the measures actually used for evaluation such as F-measure and average precision.

The area of learning structured prediction models becomes relevant in this context since MIML requires predicting a structured array of labels. The area has seen the development of powerful large-margin methods (Taskar, Guestrin, and Koller 2003) which can incorporate hidden variables (Wang and Mori 2011; Felzenszwalb et al. 2010; Yu and Joachims 2009), which is useful since MIML admits elegant formulations as a latent variable learning problem, as well as optimize non-decomposable performance measures such as F-measure (Ranjbar et al. 2013; Rosenfeld et al. 2014; Keshet 2014).

However, the only direct application of these techniques to optimize non-decomposable performance measures in the MIML setting is in the work of Haffari et al. (2015), who optimize the micro averaged F-measure in the RE setting. Their optimization algorithm interleaves the Concave-Convex Procedure (CCCP) (Yuille and Rangarajan 2001) to populate latent variables using dual decomposition (Rush and Collins 2012). This factorizes the hard optimization problem into smaller independent sub-problems over the training instances. Despite such optimization tricks and the use of heuristic local search methods replacing the exhaustive search of (Joachims 2005; Ranjbar, Vahdat, and Mori 2012)), their approach suffers from two drawbacks: (i) the resulting algorithms are slow and do not scale to large datasets and (ii) the approach does not perform well for the *heavy tail* of rare classes with small class priors.

There also has been progress in developing general purpose algorithms for the MIML problem (Zhou and Zhan 2006; Zhan and Zhou 2008) that have been applied to text and image (scene) classification tasks. The work of (Zhou and Zhan 2006) provides two methods, *viz.*, MIMLBoost and MIMLSVM for the problem. MIMLBoost solves several multi-instance single label (MISL) problems and then converts each into Single Instance Single Label (SISL) problems using multi-instance boosting. MIMLSVM, on the other hand, converts the MIML problem into several Single Instance Multi Label (SIML) problems using k-medoids clustering that uses the Hausdorff distance between all pairs of points and then solves the SIML problems using SVM. Both methods work on the degenerate versions of MIML and hence can be lossy. The main bottleneck in the MIMLSVM approach is the extremely expensive computation of Hausdorff distance matrix between all pairs of

points. As we shall see in Section 5, this causes this approach to be extremely slow. As a concluding note, we point out that the SIML approach of reducing the problem of predicting labels for bags to that of predicting labels for individual instances is very popular in RE (Zeng et al. 2015; Haffari, Nagesh, and Ramakrishnan 2015; Hoffmann et al. 2011) and MIML algorithms. We will revisit this approach while describing the MIML^{perf} algorithm.

The principles of EM, alternating minimization, *etc.*, are very popular in optimization and learning literature. We note that the classical EM algorithm cannot be directly applied to optimize multivariate performance measures as it is designed to optimize the decomposable likelihood measure over i.i.d. samples. As a result, direct adaptations of EM (Zhang and Goldman 2001) to multi-instance settings only address decomposable measures and that too, only in binary or multi-class settings where labels are exclusive. The models developed therein cannot extend directly even to decomposable performance measures in the multi-label setting since labels can co-exist in this setting, something that our approach critically exploits.

3 Problem Formulation

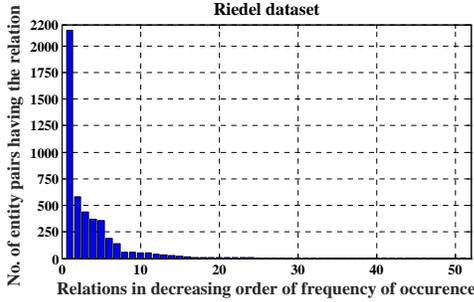
In the MIML setting, training data is presented as $\mathcal{D} := \{(\mathbf{x}_i, \mathbf{y}_i)\}_{i=1}^N$ where $\mathbf{x}_i = \{\mathbf{x}_i^{(1)}, \dots, \mathbf{x}_i^{(n_i)}\} \in \mathcal{X}$ is the i^{th} instance set (also called a *bag*) containing n_i instances and $\mathbf{y}_i = [y_{i,1}, y_{i,2}, \dots, y_{i,L}] \in \mathcal{Y} = \{0, 1\}^L$ is a vector of labels associated with \mathbf{x}_i . We will use $\mathbf{h}_i \in \{1, \dots, L, \text{nil}\}^{n_i}$ to denote the vector of *hidden* labels for \mathbf{x}_i . $h_{i,j}$ will encode whether the j^{th} instance in the bag \mathbf{x}_i expresses one of the labels $\{1, \dots, L\}$ or none (*nil*). We will denote $\mathbf{X} := \{\mathbf{x}_i\}_{i=1}^N \in \mathcal{X}$ and $\mathbf{Y} := \{\mathbf{y}_i\}_{i=1}^N \in \mathcal{Y}$.

Let us illustrate the above with an example from the RE domain. The goal here is to align facts to sentences in a large unlabeled corpus. The training data consists of *entity-pairs*, such as (Walt Disney, Mickey Mouse). For each entity pair, we are given a set of sentences (also called *mentions*) that talk about these entities, and a set of relations known to be satisfied by the pair. For instance, (Walt Disney, Mickey Mouse) satisfy the relations Co-creator-Of, Voice-Of but not the relation Animator-Of (Mickey was animated by Ub Iwerks).

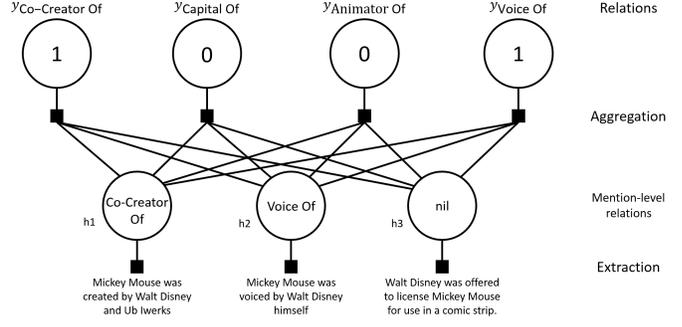
The above can be cast as an MIML problem by letting \mathbf{x}_i be the instance set or bag containing all mentions of the i -th entity pair and \mathbf{y}_i be the relations satisfied by the pair. The hidden label vector \mathbf{h}_i can then be used to denote relations expressed by individual mentions. The set of L possible relations is extracted from a knowledge-base.

We wish to learn a function $\mathbf{f} : \mathcal{X} \rightarrow \mathcal{Y}$ that predicts labels for novel data points $\mathbf{f}(\mathbf{x}) = [f^1(\mathbf{x}), f^2(\mathbf{x}), \dots, f^L(\mathbf{x})]$. Our learning process will be guided by a *performance measure* $\Delta : \mathcal{Y} \times \mathcal{Y} \rightarrow \mathbb{R}_+$. Given a dataset (\mathbf{X}, \mathbf{Y}) containing N bags, let $\mathbf{Y}^j = [y_{1,j}, y_{2,j}, \dots, y_{N,j}]$ encode which bags support label j and $\mathbf{f}^j(\mathbf{X}) = [f_j(\mathbf{x}_1), f_j(\mathbf{x}_2), \dots, f_j(\mathbf{x}_N)]$ be the vector of predictions for label j .

The simplest of performance measures is the class of *univariate* or *decomposable measures* that compute performance over a set of data points by simply averaging



(a)



(b)

Figure 1: (Left) The Riedel dataset exhibits a heavy tail in its label distribution, most relations are extremely rare. (Right) Mention level hidden labels can be used to compute the active relations for the entity-pair (Walt Disney, Mickey Mouse).

the performance on individual data points $\Delta(\mathbf{f}(\mathbf{X}), \mathbf{Y}) = \frac{1}{N} \sum_{i=1}^N \Delta(\mathbf{f}(\mathbf{x}_i), \mathbf{y}_i)$. Examples include the Hamming distance (Bi and Kwok 2013; Chen and Lin 2012), precision (Hsu et al. 2009; Weston, Bengio, and Usunier 2011), and recall (Steck 2010). Although convenient to work with and analyze, these performance measures are known to be ill suited in the presence of label imbalance or a heavy tailed label distribution (Koyejo et al. 2014; Narasimhan, Vaish, and Agarwal 2014) since they tend to neglect performance on rare labels. Incidentally, the heavy tail phenomenon is well documented in relation extraction settings (see Figure 1a).

Instead, the performance measures of choice in these situations are the *multivariate performance measures* force the predictor to do well on rare labels as well. These measures are typically *non-decomposable* as their evaluation does not decompose over individual points. In this paper we consider the family of F-measures – these have been popular for the RE problem (Haffari, Nagesh, and Ramakrishnan 2015; Surdeanu et al. 2012), as well as for label imbalanced learning in general (Koyejo et al. 2014; Ye et al. 2012).

The *label-wise* Precision and Recall of a predictor \mathbf{f} measure the performance on each individual label

$$\text{PREC}^j(\mathbf{f}; \mathbf{X}, \mathbf{Y}) := \frac{\sum_{i=1}^n y_{i,j} \cdot \mathbf{f}^j(\mathbf{x}_i)}{\sum_{i=1}^n \mathbf{f}^j(\mathbf{x}_i)}$$

$$\text{REC}^j(\mathbf{f}; \mathbf{X}, \mathbf{Y}) := \frac{\sum_{i=1}^n y_{i,j} \cdot \mathbf{f}^j(\mathbf{x}_i)}{\sum_{i=1}^n y_{i,j}}$$

whereas the global Precision and Recall calculate the overall performance of \mathbf{f} across labels

$$\text{PREC}(\mathbf{f}; \mathbf{X}, \mathbf{Y}) := \frac{\sum_{i=1}^n \sum_{j=1}^L y_{i,j} \cdot \mathbf{f}^j(\mathbf{x}_i)}{\sum_{i=1}^n \sum_{j=1}^L \mathbf{f}^j(\mathbf{x}_i)}$$

$$\text{REC}(\mathbf{f}; \mathbf{X}, \mathbf{Y}) := \frac{\sum_{i=1}^n \sum_{j=1}^L y_{i,j} \cdot \mathbf{f}^j(\mathbf{x}_i)}{\sum_{i=1}^n \sum_{j=1}^L y_{i,j}}$$

For any label j , we define label-wise F-measure as

$F_\beta^j(\mathbf{f}; \mathbf{X}, \mathbf{Y}) := \left(\frac{\beta}{\text{PREC}^j(\mathbf{f}; \mathbf{X}, \mathbf{Y})} + \frac{1-\beta}{\text{REC}^j(\mathbf{f}; \mathbf{X}, \mathbf{Y})} \right)^{-1}$, as well as the **Macro** and **Micro F-measure** as

$$F_\beta^{\text{macro}}(\mathbf{f}; \mathbf{X}, \mathbf{Y}) := \frac{1}{L} \sum_{j=1}^L F_\beta^j(\mathbf{f}; \mathbf{X}, \mathbf{Y}), \text{ and}$$

$$F_\beta^{\text{micro}}(\mathbf{f}; \mathbf{X}, \mathbf{Y}) := \left(\frac{\beta}{\text{PREC}(\mathbf{f}; \mathbf{X}, \mathbf{Y})} + \frac{1-\beta}{\text{REC}(\mathbf{f}; \mathbf{X}, \mathbf{Y})} \right)^{-1},$$

where $\beta = 0.5$ gives the standard F_1 measure. These performance measures, especially the macro F-measure, penalize predictors that perform poorly on rare labels. In the

next section, we develop scalable techniques for optimizing multivariate performance measures such as F-measure variants in the MIML and RE settings.

4 Proposed Approach

Despite having attractive properties as discussed above, multivariate performance measures such as F-measure present challenges to learning algorithms. Due to their non-decomposability, classical algorithmic tools such as online and stochastic optimization, as well as analytical tools such as uniform convergence bounds are not readily applicable.

The recent years have seen a growing interest in the problem of optimizing non-decomposable performance measures, especially F-measure variants (Dembczyński et al. 2013; Narasimhan, Kar, and Jain 2015). However, past work is mostly restricted to binary classification. An exception is the recent work of Haffari et al. (2015) that utilizes the structural SVM approach (Joachims 2005) to optimize the F-micro measure in the RE setting. However, the approach is woefully non-scalable, struggling to cope with even a few thousand data points. This severely restricts its applicability to real life and production-grade problems.

This section will develop $\text{MIML}^{\text{perf}}$, a scalable tool for optimizing multivariate performance measures in the MIML setting. $\text{MIML}^{\text{perf}}$ is based on a *plug-in* approach to classification. Plug-in classifiers have been studied in binary classification settings (Kotłowski and Dembczynski 2015; Narasimhan, Vaish, and Agarwal 2014; Koyejo et al. 2014; Ye et al. 2012) with great success. However, to the best of our knowledge, plug-in approaches have not been studied in MIML/RE settings before.

Plug-In Classifiers

Consider a simple binary classification problem where the task is to assign every data point $\mathbf{x} \in \mathcal{X}$, a binary label $y \in \{\pm 1\}$. Plug-in classifiers achieve this by first learning to predict *Class Probability Estimate* (CPE) scores. A function $g : \mathcal{X} \rightarrow \mathbb{R}_+$ is learnt such that $g(\mathbf{x}) \approx \mathbb{P}[y = 1]$. Various tools such as logistic regression may be used to learn this CPE model g . The final classifier is of the form

Algorithm 1 MIML^{perf}: Training Routine

Input: Data $\{(\mathbf{x}_i, \mathbf{y}_i)\}_{i=1}^N$, expression rate κ , perf. measure Δ

- 1: For all (i, j) such that $y_{i,j} = 1$, set random $\kappa \cdot n_i$ entries of the vector $\mathbf{z}^{(i,j)}$ to 1 // *Initialize hidden labels randomly*
- 2: **while** not converged **do**
- Step 1: Fix hidden variables, update plug-in classifiers**
- 3: **for** every label $j \in [L]$ **do**
- 4: $\mathcal{D}^j \leftarrow \{ \{(\mathbf{x}_i^{(k)}, z_k^{(i,j)})\}_{k=1}^{n_i} \}_{i=1}^n$ // *Prepare datasets*
- 5: $g^j \leftarrow \text{CPE-train}(\mathcal{D}^j)$ // *Train CPE models*
- 6: **end for**
- 7: $\boldsymbol{\eta} \leftarrow \text{Tune-thresholds}((\mathbf{X}, \mathbf{Y}), \mathbf{p}; \Delta)$ // *Optimize Δ*
- Step 2: Fix plug-in classifiers, update hidden variables**
- 8: **for** $(i, j) \in [N] \times [L]$ such that $y_{i,j} = 1$ **do**
- 9: $\mathbf{z}^{(i,j)} \leftarrow \mathbf{0}^{n_i}$ // *Reset hidden labels*
- 10: $c^{(i,j)} \leftarrow \sum_{k=1}^{n_i} \mathbb{I}\{g^j(\mathbf{x}_i^{(k)}) \geq \eta_j\}$
- 11: $S^{(i,j)} \leftarrow \text{Sample } c^{(i,j)} \text{ entries of } \mathbf{z}^{(i,j)} \text{ according to } g^j$
- 12: $z_k^{(i,j)} \leftarrow 1$ for all $k \in S^{(i,j)}$ // *Reestimate hidden labels*
- 13: **end for**
- 14: **end while**

Algorithm 2 MIML^{perf}: Testing Routine

Input: Test point $\mathbf{x} = \{\mathbf{x}^{(1)}, \dots, \mathbf{x}^{(n_t)}\}$ with n_t instances, CPE models g^1, \dots, g^L , thresholds $\boldsymbol{\eta} = [\eta_1, \dots, \eta_L]$.

- 1: **for** $k = 1, 2, \dots, n_t$ **do**
- 2: $h_k \leftarrow \{j : g^j(\mathbf{x}^{(k)}) \geq \eta_j\}$ // *Discover hidden labels*
- 3: **end for**
- 4: **for** $j = 1, 2, \dots, L$ **do**
- 5: $\hat{y}_j \leftarrow \bigvee_{k=1}^{n_t} \mathbb{I}\{j \in h_k\}$ // *Aggregation step*
- 6: **end for**
- 7: **return** $\hat{\mathbf{y}} = [\hat{y}_1, \hat{y}_2, \dots, \hat{y}_L]$

$\text{sign}(g(\mathbf{x}) - \eta)$ where η is a threshold that is tuned to maximize the performance measure being considered, e.g. classification accuracy, F-measure, G-mean etc.

Plug-in approaches offer various benefits. They can be used to optimize complex multivariate performance measures. In fact the same CPE model can be reused to target several performance measures by simply changing the threshold tuning step. Plug-in approaches have been rigorously analyzed and are known to be statistically consistent (Narasimhan, Vaish, and Agarwal 2014).

However, plug-in methods require total supervision, akin to requiring every instance in every bag to be labeled, whereas MIML operates under a significantly impoverished distant supervision setting. Thus, a direct application of existing plug-in approaches to MIML problems is not possible.

MIML^{perf}: An MIML Algorithm for Optimizing Multivariate Performance Measures

MIML^{perf} reduces the problem of predicting labels for a bag to the problem of predicting labels expressed by individual instances in that bag. Recall that this is captured by the hidden variables (see Section 3). E.g. the sentence “*Mickey Mouse was voiced by Walt Disney himself*” expresses the label `Voice Of` but not the label `Co-creator Of`. Afterward, a label is predicted as relevant for the bag if at least one instance in the bag expresses that label. This ag-

gregation or SIML approach has been standard in MIML and RE settings (Haffari, Nagesh, and Ramakrishnan 2015; Hoffmann et al. 2011; Zhan and Zhou 2008).

Existing approaches suffer since they use expensive techniques such as integer linear programming Haffari et al. (2015) to set these hidden variables. MIML^{perf} instead uses plug-in classifiers to set the hidden variables which results in training routines that are orders of magnitude faster. However, training these classifiers is challenging since we do not have any instance level supervision – the training data does not tell us which instances express which labels.

Overview of MIML^{perf} Training: MIML^{perf} overcomes the challenge of absence of instance level supervision in a scalable manner by combining two powerful approaches – plug-in classifiers and alternating optimization. At every time step, MIML^{perf} estimates the hidden variables, i.e. for each instance in a training bag, it estimates which labels are likely to be expressed by that instance. These estimates are valuable since they offer a form of instance level supervision to the method. This makes it possible for MIML^{perf} to train plug-in classifiers by learning CPE models and tuning appropriate thresholds; a separate classifier is trained for each of the L labels. MIML^{perf} uses these classifiers to get improved estimates of the hidden variables. The process is repeated for a few iterations. Details of the training and testing routines for MIML^{perf} are given in Algorithms 1 and 2.

Hidden Variables These are used to record the algorithm’s beliefs about which labels are expressed by individual instances. For a set of N data points $\{(\mathbf{x}_i, \mathbf{y}_i)\}_{i=1}^N$, the binary variable $z_k^{(i,j)} \in \{0, 1\}$ indicates whether the k^{th} instance in the i^{th} bag expresses the j^{th} label or not. If the i^{th} data point has n_i instances then the vector $\mathbf{z}^{(i,j)} \in \{0, 1\}^{n_i}$ encodes which of the instances in the bag express the label j . A crucial observation that makes our approach scalable is that if a bag does not have a label j , then none of its instance can express it. In other words, if $y_{i,j} = 0$ then $\mathbf{z}^{(i,j)} = \mathbf{0}$. This observation is valuable since we need only worry about $z_k^{(i,j)}$ when $y_{i,j} = 1$. Since most bags have very few labels (see Figure 1a), this introduces sparsity into our approach. We now describe the alternation steps.

Step 1: Learning Plug-In Classifiers Given an assignment to all the hidden variables $\mathbf{z}^{(i,j)}$, MIML^{perf} learns a plug-in classifier for each label. The job of these classifiers corresponding to a particular label is to predict whether a given instance expresses that label or not. This is done by simply formulating a binary classification problem for each label with the hidden variables acting as the “classes”. A standard procedure like logistic regression (CPE-train in Algorithm 1) is used to obtain CPE models, one for each label. Afterward, thresholds are tuned for each label such that the performance measure Δ being targeted, such as F-macro or F-micro measure, is maximized. Doing so in an efficient manner is challenging as in large scale settings, the number of CPE scores being handled can run into millions or more.¹

Step 2: Re-estimating Hidden Variables The CPE mod-

¹We refer the reader to <https://www.cse.iitb.ac.in/~ganesh/papers/supp-aaa17/> for details.

els learnt in the previous step can be used to obtain (noisy) CPE scores for all instances with respect to all labels. The noise is due to incorrect assignments to the hidden variables in the previous step. Nevertheless, this gives us an estimate of which instances are more likely to express a certain label. $MIML^{perf}$ uses these CPE scores to reassign the hidden variables. In order to avoid trusting these scores completely, $MIML^{perf}$ chooses a random set of instances with high CPE scores with respect to a label and assigns them that label. This has the effect of reinforcing good CPE models as well as smoothing out errors. For the initialization step, if a bag has a label j , the method assigns a random κ fraction of instances in that bag to label j . κ is an *expression rate* parameter that is only used for initialization.

Overview of $MIML^{perf}$ Training: The testing procedure of $MIML^{perf}$ (see Algorithm 2) involves simply applying the plug-in classifiers and performing the aggregation step to obtain the predictions for all labels for a bag. This procedure is enormously cheaper than the integer linear programming approach followed by Haffari et al. (2015).

Theoretical Analysis

Giving strong theoretical guarantees for algorithms for non-convex learning problems such as multi-instance learning is a challenging albeit interesting problem. We are nevertheless able to establish generalization guarantees for our method which proves that our method does not overfit. Let $\hat{\mathbf{f}}$ be the classifier generated by $MIML^{perf}$. Let the training and test sets (\mathbf{X}, \mathbf{Y}) and $(\mathbf{X}^t, \mathbf{Y}^t)$ be chosen randomly from some fixed but unknown distribution. Let π denote the minimum frequency of any label.

Theorem 1. *Let the instances be represented as d dimensional features $\mathbf{x}_i^{(k)} \in \mathbb{R}^d$. Then for any N such that $\sqrt{\frac{1}{N} (\log \frac{1}{\delta} + d \log \frac{N}{d})} < c \cdot \pi$ for a small constant c , we have with probability at least $1 - \delta$, for some constant C ,*

$$\left| \mathbb{E} \left[F_{\beta}^{macro}(\hat{\mathbf{f}}; \mathbf{X}^t, \mathbf{Y}^t) \right] - F_{\beta}^{macro}(\hat{\mathbf{f}}; \mathbf{X}, \mathbf{Y}) \right| \leq \sqrt{\frac{C}{N} (d + \log \frac{1}{\delta})}$$

The result is stated for linear models for sake of simplicity and can be extended to hypothesis spaces with finite capacity as well. A similar result holds for F-micro measure as well.

5 Experiments

We present detailed comparisons of our approach with the state of the art on three benchmark MIML/RE datasets.

1. **Riedel Distant Supervision Dataset:** For the distantly supervised relation extraction problem, we use the benchmark dataset created by (Riedel, Yao, and McCallum 2010). The dataset was created by aligning relations from *Freebase*² with the sentences in the *New York Times* corpus (Sandhaus 2008). The labels for the data points come from the Freebase database; however, Freebase is incomplete (Ritter et al. 2013). A data point is labeled *nil* when either no relation exists or the relation is absent in Freebase. Following (Haffari, Nagesh, and Ramakrishnan

Table 1: Dataset Statistics

	#bags	#labels	labels point	points label	instances bag
Riedel	4350	52	1.08	90.4	6.6
Scene	2000	5	1.24	494.4	9
Reuters	2000	7	1.15	329.71	3.56

2015), we train and evaluate all algorithms on a subset of this dataset, termed as the *positive dataset*, which consists of only non-*nil* relation labeled data points.

2. **MIML Scene Classification Dataset (Scene):** The Scene data set contains 2000 scene images collected from the COREL image collection and the Internet, with five different possible class labels, *viz.*, *desert*, *mountains*, *sea*, *sunset* and *trees*. Each image is represented as a bag of nine instances with each instance represented as 15 dimensional feature vector that corresponds to an image patch. Following MIMLSVM, We divided the data into two parts consisting of 1600 data points for training and the remaining 400 points for testing.
3. **MIML Text Classification Dataset (Reuters):** The text data is derived from the widely studied Reuters-21578 collection using seven most frequent classes. It consists of 2000 documents with 15% associated with more than one class labels. In this dataset each instance is represented as a 243-dimensional feature vector and corresponds to a text segment. Again, we follow MIMLSVM in the way we partition this dataset into training and testing splits.

Comparisons against existing approaches We compare $MIML^{perf}$ against state-of-the-art methods for each of the three datasets. We report F_{β}^{macro} , F_{β}^{micro} and average precision as our evaluation measures. In addition, we also report the training time and the average time required to predict labels for each test bag (instance set). We used a default value $\kappa = 1$ as the *prevalence parameter* for training $MIML^{perf}$. For the sake of fairness, training splits and feature sets were kept common across all comparative experiments.

Table 2 compares $MIML^{perf}$ against state-of-the-art approaches MIMLSVM and M3MIML (Zhan and Zhou 2008) for the Scene and Reuters datasets. We observe that $MIML^{perf}$ consistently outperforms both methods on all three evaluation measures. Additionally, as noted in Table 5, $MIML^{perf}$ is significantly and consistently faster in training than MIMLSVM and even more so at testing time.

Table 3 compares $MIML^{perf}$ on the distant supervision RE setting with the MM- F_{β} approach (Haffari, Nagesh, and Ramakrishnan 2015). We note that $MIML^{perf}$ offers significant improvements over MM- F_{β} on F-macro along with a 145-fold speedup in training. The gains on F-micro are marginal. However, in skewed class distribution settings, F-macro is a more relevant measure of performance than F-micro..

In addition to offering gains on training and test speeds, our approach does not require the entire dataset to be loaded in memory. As noted earlier, $MIML^{perf}$ is executed by making several passes over the data and is inherently streaming in nature. None of the other approaches we have compared against, enjoy these properties.

²www.freebase.com

Table 2: Performance of $MIML^{perf}$ compared against MIMLSVM and M3MIML on the Scene and Reuters Datasets

Dataset	Kernel	F-Macro			F-Micro			Avg. Precision		
		MIMLSVM	M3MIML	$MIML^{perf}$	MIMLSVM	M3MIML	$MIML^{perf}$	MIMLSVM	M3MIML	$MIML^{perf}$
Scene	lin	0.4292	0.386	0.5427	0.4475	0.3868	0.5287	0.6635	0.5754	0.7465
	rbf	0.6054	0.5872	0.6201	0.6016	0.5796	0.6158	0.7704	0.74857	0.7919
Reuters	lin	0.8274	0.7601	0.8492	0.8395	0.8067	0.8629	0.9489	0.9463	0.9625
	rbf	0.8839	0.6998	0.8901	0.8689	0.7866	0.8942	0.9467	0.9403	0.9706

Table 3: $MIML^{perf}$ comparison with the $(MM-F_\beta)$ model by Haffari et. al. on the Riedel dataset

	F-macro	Precision	Recall	F-micro	Train time
MM- F_β	0.1366	0.6599	0.6521	0.6559	4h 20m
$MIML^{perf}$	0.2283	0.7928	0.5781	0.6686	1m 49s

Table 4: Effect of the training objective on test performance on the Riedel dataset

	F-macro	F-micro
Optimizing F_β^{macro}	22.8354	61.0615
Optimizing F_β^{micro}	18.984	66.8648

Table 5: Comparisons of training time and testing time per instance

Dataset	Kernel	Training time			Testing time per instance		
		MIMLSVM	$MIML^{perf}$	Speedup	MIMLSVM	$MIML^{perf}$	speedup
Scene	Linear	7m 45s	1.66s	280×	0.0920s	0.0009s	102×
	RBF	9m 24s	6m 40s	1.41×	0.0921s	0.03s	3×
Reuters	Linear	3m 55s	1.62s	145×	0.1035s	0.0005s	207×
	RBF	5m 04s	1m 02s	5×	0.1063s	0.008s	13×

Table 6: Relation-wise comparisons of F-score with $MM-F_\beta$, $MIML^{perf}$, $\kappa = 1$ and $MIML^{perf}$, tuned κ on Riedel

Relation	% of occurrence	MM- F_β	$MIML^{perf}$ $\kappa = 1$	$MIML^{perf}$ tuned κ
/people/person/place_lived	12.36	0.15966	0.46556	0.46897
/people/deceased_person/place_of_death	4.04	0.19231	0.31111	0.35294
/location/administrative_division/country	1.26	0	0.37624	0.37624
/business/company/founders	1.09	0.48148	0.68571	0.75676
/location/country/capital	0.77	0	0.10866	0.11494
/film/film/featured_film_locations	0.15	0	0.01262	0.01325
Overall F-Macro		0.13660	0.22835	0.23282

Effects of changes in parameters and objective In Table 4 we compare the difference in performances of $MIML^{perf}$ when the macro-F measure is replaced with the micro-F measure as the objective. We compare the results of training to optimize the F_β^{micro} measure against optimizing F_β^{macro} . In each setting, we report both F_β^{micro} and F_β^{macro} . We note the strong correspondence between the choice of performance in the training objective and performance being evaluated upon the test dataset.

We expect optimizing the F-macro performance measure to enhance performance on the rarer classes (that have low priors). We confirm this in Table 6 which compares the performance of $MIML^{perf}$ with $MM-F_\beta$ for some of the rarer classes. Whereas $MM-F_\beta$ reports extremely low F-scores (in some cases 0) on these rare classes, $MIML^{perf}$ performs much better, even with $\kappa = 1$. The value of κ yielding the best performance for a class changes across classes and therefore, also report results with κ tuned for each class on the training dataset. This gives us even better gains.

We also test for statistical differences between the accuracies of $MIML^{perf}$ and $MM-F_\beta$ on all the 29 classes using the

Wilcoxon³ signed-rank test. We notice that the sum of the signed ranks (222 with $\kappa = 1$ and 237 for κ tuned for each class) is very clearly in favour of $MIML^{perf}$ over $MM-F_\beta$.

6 Conclusions

We proposed $MIML^{perf}$, a scalable approach for optimizing several multivariate performance measures in the MIML setting and applied it to relation extraction and other MIML tasks. Our approach makes novel use of the *plug-in* technique, offers significantly reduced running times, and caters well even to rare classes, without compromising on the popular ones. Furthermore, our approach appears very amenable to distributed and parallel computing and a possible future work is validating this hypothesis.

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³The signed ranks for the 29 classes of the Riedel dataset are available as a spreadsheet at <https://www.cse.iitb.ac.in/~ganesh/papers/supp-aaai17/>.

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